FRACTURE MECHANICS CRITICAL ASSESSMENT OF THE STEEL STRUCTURES JOINTS

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Summary: Elaboration of a methodology for determining the acceptability of detected cracks/flaws in a structure, has a major practical importance in the overall assessment and life integrity of a structure. The relation given by fracture mechanics links a parameter which describes the stress intensity at a crack tip to a material characteristic – fracture toughness. This relation provides the possibility of assessing the fracture conditions of the structural elements with defects (cracks) [1].

The present paper is proposing assessing the structural elements welded joints from the fracture mechanics point of view. The analysis is carried out in accordance with the British Standard procedure BS 7910 (‘Guide to methods for assessing the acceptability of flaws in metallic structures’)[5]

Keywords: Fracture mechanics, steel structures, structural integrity

1. INTRODUCTION

Most welding fabrication codes specify maximum tolerable flaw sizes and minimum tolerable Charpy energy, based on good workmanship, i.e. what can reasonably be expected within normal working practices. These requirements tend to be somewhat arbitrary, and failure to achieve them does not necessarily mean that the structure is at risk of failure. An Engineering Critical Assessment (ECA) is an analysis, based on fracture mechanics principles, of whether or not a given flaw is safe from brittle fracture, fatigue, creep or plastic collapse under specified loading conditions. An ECA can be used: during design, to assist in the choice of welding procedure and/or inspection techniques; during fabrication, to assess the significance of: a) known defects which are unacceptable to a given code [2], or b) a failure to meet the toughness requirements of a fabrication code; during operation, to assess flaws found in service and to make decisions as to whether they can safely remain, or whether down-rating/repair are necessary. This type of assessing can be done if the following elements are known: material fracture toughness, geometry and size of the crack, resulted stresses from the applied forces.

The fracture mechanics based methodologies are permitting the following types of assessments:

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- Maximal crack dimension assessment to which the structural element will not fail, named also the admissible crack dimension; for this type of assessing is needed the maximal stresses values and the value of the material fracture toughness;
- Maximal stress value assessment to which the structural element with a crack will not fail
- Minimal fracture toughness value assessment to the structural element with a crack; this assessment needs knowing the maximal stress value and the admissible crack dimensions.

Considering a simple case – a steel plate under tension (figure 1), can be underlined the following types of fracture: Brittle fracture – controlled by the value of the applied tension force, dimension of the crack, material fracture toughness and geometry of the element; Plastic fracture – the net section in which the yielding phenomena appears, controlled by the applied tension force value, the yielding limit and the element geometry; Rupture as a result of extended material yielding, controlled by the applied tension force, crack size, material fracture toughness and the element geometry.

Figure 1. Describing fracture – plate under tension

The transition domain between these types of fracture is governed by the interaction between the brittle fracture and the plastic failure. This is expressed through a dependency relation of two parameters $K_r$ and $S_r$. These parameters are defined based on the geometrical dimensions of the structural element, crack dimensions and geometry, stresses that appear in the cross section following the applied loads, taken into account the fracture toughness of the material $K_{mat}$.

2. FAILURE ASSESSMENT DIAGRAMS – FAD 2

The Failure Assessment Diagram (FAD) describes the interaction between the brittle fracture and plastic failure through a $F_f = f(S_r)$ function.

Structures using reasonably tough materials (high $K_{ic}$) and having only small cracks (low $K$) will lie in the strength-of-materials regime. Conversely, if the material is brittle (low $K_{ic}$) and strong $S_r$ (high yield strength), the presence of even a small crack is likely to trigger fracture. Thus, the fracture mechanics assessment is a crucial one. The special circumstances that would be called into play in the upper right corner of figure 2 in this regime, a cracked structure would experience large-scale plastic deformation prior to crack extension.
The level 2 (FAD-2) assessment is the normal evaluation path for general application. The method is presenting an assessment line given by an equation of a curve and a cut-off line. If the assessment point is in the interior of the surface limited by the assessment line, the flaw is acceptable and if the assessment point is at the outside area, the flaw is considered unacceptable.

The equations which are describing the assessment line are:

\[ \sqrt{\delta_r} \text{ or } K_r = \left( \frac{1}{14} \frac{L_r^2}{L_r^2 + 0.3 + 0.70 \exp(-0.65L_r^2)} \right) \text{ for } L_r \leq L_{r\text{max}} \]  
\[ \sqrt{\delta_r} \text{ or } K_r = 0 \text{ for } L_r > L_{r\text{max}} \]  

The cut-off line is fixed in point where \( L_r = L_{r\text{max}} \) where:

\[ L_{r\text{max}} = \left( \sigma_Y + \sigma_u \right) / (2 \sigma_Y) \]  

in which:

\( \sigma_Y \) – the yielding resistance of the material 
\( \sigma_u \) – the ultimate resistance of the material

For the assessment on level 2 FAD is necessary to pass through the following phases [4]:

- Determining the stresses – following a structural analysis. The assessments are considering the real distribution of the stresses in the proximity of the flaws – \( P_m, P_b, Q_m \) and \( Q_b \).
- The fracture ratio \( K_r \) must be determined

\[ K_r = K_f / K_{\text{mat}} \]  

in which \( K_{\text{mat}} \) represents the fracture toughness of the assessed material, determined at the service temperature.

The stress intensity factor (SIF) – \( K_i \) is determined with the following relation:

\[ K_i = (Y \cdot \sigma) \cdot (\pi \cdot a)^{1/2} \]  

where

\[ Y \cdot \sigma = (Y \cdot \sigma)_p + (Y \cdot \sigma)_s \]  

Figure 2. General plot of the ratios of the toughness and stress showing the relationship between linear elastic fracture mechanics and strength of materials as it relates to fracture and structural integrity [3]
in which:
\[
(Y\cdot\sigma)_P = M\cdot f_w \cdot \left(k_{tm} \cdot M_{m} \cdot M_{m} + k_{tb} \cdot M_{b} \cdot M_{b} \cdot [P_{b} + (k_m - 1)P_{m}] \right) \\
(Y\cdot\sigma)_S = M_{m} \cdot Q_{m} + M_{b} \cdot Q_{b}
\]  
(7)  
(8)

- Determining the ratio of stress \(L_r\) according with:
\[
L_r = \sigma_{ref} / \sigma_Y
\]
(9)

As a study case, there is presented an existing structure – wind turbine column. Following visual inspection and NDT testing, there were discovered several flaws – cracklike type. An indepth study was needed in order to conclude upon the realibility and safety of the structure. In case of assessment level 2 – FAD-2, there were done assessments on different flaws type and flaws position for the in case. The values of the input data are:
- \(\sigma_Y\) (yield strength)= 355 MPa; \(\sigma_T\) (ultimate strength)= 510 MPa; S355J2 steel type
- \(K_{mat} = 81.8\) MPa m\(^{1/2}\) was determined on the specimens (through testing)
- \(P_m = 251\) MPa - Primary stress - determined following a structural analysis
- \(k_{tm} = 1; k_{tb} = 1\) (stress concentrators factors)
- \(Q_{tm} = 0\) (thermal membrane stress) and \(Q_{tb} = 0\) (thermal bending stress)
- \(Q_{m} = 0\) (residual membrane stress) and \(Q_{b} = 0\) (residual bending stress)

### Table 1 – Flaw cases description

<table>
<thead>
<tr>
<th>Case no.</th>
<th>Name</th>
<th>Flaw type</th>
<th>Description of the flaw</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>(TTF-1)</td>
<td>through thickness flaw</td>
<td>Crack in the tube wall in the proximity of the welded joint</td>
</tr>
<tr>
<td>Case 2</td>
<td>(TTF-2)</td>
<td>through thickness flaw</td>
<td>Crack in the welding longitudinal direction</td>
</tr>
<tr>
<td>Case 3</td>
<td>(TTF-3)</td>
<td>through thickness flaw</td>
<td>Crack in the welding transversal direction</td>
</tr>
<tr>
<td>Case 4</td>
<td>(TTF-4)</td>
<td>through thickness flaw</td>
<td>Crack in the flange of the segment joint in proximity of the welding longitudinal direction</td>
</tr>
<tr>
<td>Case 5</td>
<td>(TTF-5)</td>
<td>through thickness flaw</td>
<td>Crack in the flange of the segment joint in proximity of the welding transversal direction</td>
</tr>
<tr>
<td>Case 6</td>
<td>(EF-1)</td>
<td>edge flaw</td>
<td>Crack in the tube wall in the proximity of the welded joint</td>
</tr>
<tr>
<td>Case 7</td>
<td>(EF-2)</td>
<td>edge flaw</td>
<td>Crack in the welding longitudinal direction</td>
</tr>
<tr>
<td>Case 8</td>
<td>(EF-3)</td>
<td>edge flaw</td>
<td>Crack in the welding transversal direction</td>
</tr>
<tr>
<td>Case 9</td>
<td>(EF-4)</td>
<td>edge flaw</td>
<td>Crack in the flange of the segment joint in proximity of the welding longitudinal direction</td>
</tr>
<tr>
<td>Case 10</td>
<td>(EF-5)</td>
<td>edge flaw</td>
<td>Crack in the flange of the segment joint in proximity of the welding transversal direction</td>
</tr>
</tbody>
</table>
Considering the position of the flaw regarding the stress direction and position in the assembly of the steel shell element, it resulted 10 types of assessed flaws as presented in table 1.

The flaws were considered as present in the steel shell elements. In a conservative manner, the W dimension at some part of the flaws types was considered 200mm, taken into account that the area of tension from the segment joint of the steel pillar, is about 200mm. Increasing the W dimension will decrease the safety of the structure in the area of the joint.

Table 2 - FAD 2 – in case - flaws assessed: geometry and results (with corresponding figures and flaw name – figure 3 and 4)

<table>
<thead>
<tr>
<th>Fig. no.</th>
<th>Case</th>
<th>B</th>
<th>W</th>
<th>2a</th>
<th>a</th>
<th>2c</th>
<th>p</th>
<th>r₀</th>
<th>h</th>
<th>t₀</th>
<th>L₀</th>
<th>Kᵣ</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>FP-TTF-1</td>
<td>16</td>
<td>200</td>
<td>30</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td>0.831</td>
</tr>
<tr>
<td></td>
<td>FP-TTF-2</td>
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<td>200</td>
<td>30</td>
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<td>0.831</td>
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</tr>
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<td>FP-TTF-4</td>
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<td>200</td>
<td>30</td>
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<td>0.831</td>
</tr>
<tr>
<td></td>
<td>FP-TTF-5</td>
<td>25</td>
<td>120</td>
<td>30</td>
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<td>0.942</td>
</tr>
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<td>4</td>
<td>FP-EF-1</td>
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<td>15</td>
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<td>0.7644</td>
</tr>
<tr>
<td></td>
<td>FP-EF-2</td>
<td>32.63</td>
<td>200</td>
<td>15</td>
<td></td>
<td></td>
<td></td>
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<td>0.7644</td>
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<td>FP-EF-3</td>
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<td>32.63</td>
<td>15</td>
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<td>0.7644</td>
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<td></td>
<td>FP-EF-5</td>
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<td>120</td>
<td>15</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>0.8080</td>
</tr>
</tbody>
</table>

Figure 3. FP-TTF – Group of flaws - assessment
5. Международна конференција
Савремена достижности у грађевинарству 21. април 2017. Суботица, СРБИЈА

With the presented procedure, further assessment can be made on the joint and steel shell element taken into account different dimensions. Figure 4 and 5 shows the assessment of the flaws grouped. It can be seen that the FP-TTF 5 – through thickness flaw – crack of 30mm in the flange of the segment joint is a critical flaw – the assessment point is in the unsafe area of the diagram. Also the FP EF 5 – edge flaw in the flange of the segment joint is a critical flaw – t15mm flaw is putting under risk the joint and the structure.

3. DETERMINING THE CRITICAL VALUE OF THE FLAW

Determining the critical value of the flaws is important because it serves to a limit value for fatigue further analysis based on fracture mechanics principles, needed for

![Figure 5. FP-TTF-1 critical flaw](image1)

![Figure 6. FP-TTF-2 critical flaw](image2)
Figure 7. FP-TTF-3 critical flaw

Figure 8. FP-TTF-4 critical flaw

Figure 9. FP-TTF-5 critical flaw

Figure 10. FP-EF-1 critical flaw

Figure 11. FP-EF-2 critical flaw

Figure 12. FP-EF-3 critical flaw
determining the number of cycles for a crack to extend from an initial dimension to a critical dimension which means the failure of the element.
The procedure uses FAD-2 assessment data, and it gives the critical dimension of the crack.
The input data is the same as for FAD-2 assessment. The results are presented in table 3. The critical dimension of the crack for each case are represented in figures 5 to 14.

Table 3. - FAD 2 – critical dimension of the flaw (with corresponding figures and flaw name)

<table>
<thead>
<tr>
<th>Case name</th>
<th>B</th>
<th>W</th>
<th>(2a_o)</th>
<th>(a_o)</th>
<th>(2c_0)</th>
<th>(p_0)</th>
<th>(r_0)</th>
<th>(h_0)</th>
<th>(t_w)</th>
<th>Flaw Height Critical</th>
<th>Flaw Length Critical</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 FP-TTF-1</td>
<td>16</td>
<td>200</td>
<td>30</td>
<td>N/A</td>
<td>36.249</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>2 FP-TTF-2</td>
<td>32.6</td>
<td>200</td>
<td>30</td>
<td>N/A</td>
<td>36.249</td>
<td></td>
<td></td>
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<tr>
<td>3 FP-TTF-3</td>
<td>200</td>
<td>32.6</td>
<td>10</td>
<td>N/A</td>
<td>11.330</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>4 FP-TTF-4</td>
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<td>200</td>
<td>30</td>
<td>N/A</td>
<td>36.243</td>
<td></td>
<td></td>
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<tr>
<td>5 FP-TTF-5</td>
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<td>120</td>
<td>30</td>
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</tr>
<tr>
<td>6 FP-EF-1</td>
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<td>200</td>
<td>15</td>
<td>N/A</td>
<td>17.230</td>
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</tr>
<tr>
<td>7 FP-EF-2</td>
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<td>200</td>
<td>15</td>
<td>N/A</td>
<td>17.230</td>
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</tr>
<tr>
<td>8 FP-EF-3</td>
<td>200</td>
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<td>5</td>
<td>N/A</td>
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<tr>
<td>9 FP-EF-4</td>
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<td>200</td>
<td>15</td>
<td>N/A</td>
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<td>120</td>
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<td>N/A</td>
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</tbody>
</table>

Conclusions and discussions on the results
There were assessed ten types of flaws (through thickness flaw and edge flaw) which were discovered in the wind turbine pillar – in the welded joint of the segment connection,
nearby the welded joint, in the flange of the segment joint. Different types of locations were taken into account thus resulting groups of flaws which were assessed and compared. The input data took into account the results from the FEM analysis of structure and the experimental results for material properties, all needed in the assessment procedures.

The comparison of the flaws assessment with fracture mechanics procedures, revealed several problems:
- Sensibility of the joints to the through thickness flaw in the endplate of the segment joint (FP-TTF-5). In case of a only 30mm flaw the element is considered unsafe.
- The edge flaw type – FP-EF-3 (flaw in the fillet welding of the shell element and the endplate – segment joint), is the most dangerous – a 15mm crack depth into welded joint is a critical flaw for which the joint is considered unsafe.

REFERENCES